

**System and Method for Automated Experience Rating and/or Loss  
Reserving**

The invention relates to a system and a method for automated experience rating and/or loss reserving, a certain event  $P_{if}$  of an initial time interval  $i$  with  $f=1, \dots, F_i$  for a sequence of development intervals  $k=1, \dots, K$  including development values  $P_{ikf}$ . For the events  $P_{1f}$  of the first initial time interval  $i=1$ , all development values  $P_{1kf}$   $f=1, \dots, F_1$  are known. The invention relates particularly to a computer program product for carrying out this method.

Experience rating relates in the prior art to value developments of parameters of events which take place for the first time in a certain year, the incidence year or initial year, and the consequences of which propagate over several years, the so-called development years. Expressed more generally, the events take place at a certain point in time, and develop at given time intervals. Furthermore, the event values of the same event demonstrate over the different development years or development time intervals a dependent, retrospective development. The experience rating of the values takes place through extrapolation and/or comparison with the value development of known similar events in the past.

A typical example in the prior art is the several years' experience rating based upon damage events, e.g., of the payment status  $Z$  or the reserve status  $R$  of a damage event at insurance companies or reinsurers. In the experience rating of damage events, an insurance company knows the development of every single damage event from the time of the advice of damage up to the current status or until adjustment. In the case of experience rating, the establishment of the classic credibility formula through a stochastic model dates from about 30 years ago; since then, numerous variants of the model have been developed, so that today an actual credibility theory may be spoken of. The chief problem in the application of credibility formulae consists of the unknown parameters which are determined by the structure of the portfolio. As an alternative to known methods of estimation, a game-theory approach is also offered in the prior art, for instance: the actuary or insurance statistician knows bounds for the parameter, and determines the optimal

premium for the least favorable case. The credibility theory also comprises a number of models for reserving for long-term effects. Included are a variety of reserving methods which, unlike the credibility formula, do not depend upon unknown parameters. Here, too, the prior art comprises methods by stochastic  
 5 models which describe the generation of the data. A series of results exist above all for the chain-ladder method as one of the best known methods for calculating outstanding payment claims and/or for extrapolation of the damage events. The strong points of the chain-ladder method are its simplicity, on the one hand, and, on the other hand, that the method is nearly distribution-free,  
 10 i.e., the method is based on almost no assumptions. Distribution-free or non-parametric methods are particularly suited to cases in which the user can give insufficient details or no details at all concerning the distribution to be expected (e.g., Gaussian distribution, etc.) of the parameter to be developed.

The chain-ladder method means that of an event or loss  $P_{if}$  with  $f=1, 2, \dots, F_i$  from incidence year  $i=1, \dots, I$ , values  $P_{ikf}$  are known, wherein  $P_{ikf}$  may be, e.g., the payment status or the reserve status at the end of each handling year  $k=1, \dots, K$ . Therefore, an event  $P_{if}$  consists in this case in a sequence of dots

$$P_{if} = (P_{i1f}, P_{i2f}, \dots, P_{iKf})$$

of which the first  $K+1-i$  dots are known, and the yet unknown dots  
 20  $(P_{i,K+2-1,f}, \dots, P_{i,K,f})$  are to be predicted. The values of the events  $P_{if}$  form a so-called loss triangle or, more generally, an event-values triangle

$$\begin{pmatrix} P_{11f=1..F_1} & P_{12f=1..F_1} & P_{13f=1..F_1} & P_{14f=1..F_1} & P_{15f=1..F_1} \\ P_{21f=1..F_2} & P_{22f=1..F_2} & P_{23f=1..F_2} & P_{24f=1..F_2} & \\ P_{31f=1..F_3} & P_{32f=1..F_3} & P_{33f=1..F_3} & & \\ P_{41f=1..F_4} & P_{42f=1..F_4} & & & \\ P_{51f=1..F_5} & & & & \end{pmatrix}$$

The lines and columns are formed by the damage-incidence years and the handling years. Generally speaking, e.g., the lines show the initial  
 25 years, and the columns show the development years of the examined events, it also being possible for the presentation to be different from that. Now, the chain-ladder method is based upon the cumulated loss triangles, the entries  $C_{ij}$

of which are, e.g., either mere loss payments or loss expenditures (loss payments plus change in the loss reserves). Valid for the cumulated array elements  $C_{ij}$  is

$$C_{ij} = \sum_{f=1}^{F_i} P_{ijf}$$

5 from which follows

$$\begin{pmatrix} \sum_{f=1}^{F_1} P_{11f} & \sum_{f=1}^{F_1} P_{12f} & \sum_{f=1}^{F_1} P_{13f} & \sum_{f=1}^{F_1} P_{14f} & \sum_{f=1}^{F_1} P_{15f} \\ \sum_{f=1}^{F_2} P_{21f} & \sum_{f=1}^{F_2} P_{22f} & \sum_{f=1}^{F_2} P_{23f} & \sum_{f=1}^{F_2} P_{24f} & \\ \sum_{f=1}^{F_3} P_{31f} & \sum_{f=1}^{F_3} P_{32f} & \sum_{f=1}^{F_3} P_{33f} & & \\ \sum_{f=1}^{F_4} P_{41f} & \sum_{f=1}^{F_4} P_{42f} & & & \\ \sum_{f=1}^{F_5} P_{51f} & & & & \end{pmatrix}$$

From the cumulated values interpolated by means of the chain-ladder method, the individual event can also again be judged in that a certain distribution, e.g., typically a Pareto distribution, of the values is assumed. The

10 Pareto distribution is particularly suited to insurance types such as, e.g., insurance of major losses or reinsurers, etc. The Pareto distribution takes the following form

$$\Theta(x) = 1 - \left( \frac{x}{T} \right)^\alpha$$

wherein  $T$  is a threshold value, and  $\alpha$  is the fit parameter. The

15 simplicity of the chain-ladder method resides especially in the fact that for application it needs no more than the above loss triangle (cumulated via the development values of the individual events) and, e.g., no information concerning reporting dates, reserving procedures, or assumptions concerning possible distributions of loss amounts, etc. The drawbacks of the chain-ladder

20 method are sufficiently known in the prior art (see, e.g., Thomas Mack,

*Measuring the Variability of Chain Ladder Reserve Estimates*, submitted CAS Prize Paper Competition 1993, Greg Taylor, Chain Ladder Bias, Centre for Actuarial Studies, University of Melbourne, Australia, March 2001, pp 3). In order to obtain a good estimate value, a sufficient data history is necessary. In particular, the chain-ladder method proves successful in classes of business such as motor vehicle liability insurance, for example, where the differences in the loss years are attributable in great part to differences in the loss frequencies since the appraisers of the chain-ladder method correspond to the maximum likelihood estimators of a model by means of modified Poisson distribution. Hence caution is advisable, e.g., in the case of years in which changes in the loss amount distribution are made (e.g., an increase in the maximum liability sum or changes in the retention) since these changes may lead to structural failures in the chain-ladder method. In classes of business having extremely long run-off time--such as general liability insurance--the use of the chain-ladder method likewise leads in many cases to usable results although data, such as a reliable estimate of the final loss quota, for example, are seldom available on account of the long run-off time. However, the main drawback of the chain-ladder method resides in the fact that the chain-ladder method is based upon the cumulated loss triangle, i.e., through the cumulation of the event values of the events having the same initial year, essential information concerning the individual losses and/or events is lost and can no longer be recovered later on.

Known in the prior art is a method of T. Mack (Thomas Mack, *Schriftreihe Angewandte Versicherungsmathematik*, booklet 28, pp. 310ff., Verlag Versicherungswirtschaft E.V., Karlsruhe 1997) in which the values can be propagated, i.e., the values in the loss triangle can be extrapolated without loss of the information on the individual events. With the Mack method, therefore, using the complete numerical basis for each loss, an individual IBNER reserve can be calculated (IBNER: Incurred But Not Enough Reported). IBNER demands are understood to mean payment demands which are either over the predicted values or are still outstanding. The IBNER reserve is useful especially for experience rating of excess of loss reinsurance contracts, where the reinsurer, as a rule, receives the required individual loss data, at least for the relevant major losses. In the case of the reinsurer, the temporal

development of a portfolio of risks describes through a risk process in which the damage figures and loss amounts are modeled, whereby in the excess of loss reinsurance, upon the transition from the original insurer to the reinsurer, the phenomenon of the accidental dilution of the risk process arises; on the other hand, through reinsurance, portfolios of several original insurers are combined and risk processes thus caused to overlap. The effects of dilution and overlapping have, until now, been examined above all for Poisson risk processes. For insurance/reinsurance, experience rating by means of the Mack method means that of each loss  $P_{if}$ , with  $f=1,2,\dots,F_i$  from incidence year or initial year  $i=1,\dots,I$ , the payment status  $Z_{ikf}$  and the reserve status  $R_{ikf}$  at the end of each handling year or development year  $k=1,\dots,K$  until the current status  $(Z_{i,K+1-i,f}, R_{i,K+1-i,f})$  is known. A loss  $P_{if}$  in this case therefore consists of a sequence of dots

$$P_{if} = (Z_{i1f}, R_{i1f}), (Z_{i2f}, R_{i2f}), \dots, (Z_{iKf}, R_{iKf})$$

at the payment reserve level, of which the first  $K+1-i$  dots are known, and the still unknown dots  $(Z_{i,K+2-i,f}, R_{i,K+2-i,f}), \dots, (Z_{i,K,f}, R_{i,K,f})$  are supposed to be predicted. Of particular interest is, naturally, the final status  $(Z_{i,K,f}, R_{i,K,f})$ ,  $R_{i,K,f}$  being equal to 0 in the ideal case, i.e., the claim is regarded as completely settled; whether this can be achieved depends upon the length  $K$  of the development period considered. In the prior art, as e.g. in the Mack method, a claim status  $(Z_{i,K+1-i,f}, R_{i,K+1-i,f})$  is continued as was the case in similar claims from earlier incidence years. In the conventional methods, therefore, it must be determined, for one thing, when two claims are "similar," and for another thing, what it means to "continue" a claim. Furthermore, besides the IBNER reserve thus resulting, it must be determined, in a second step, how the genuine belated claims are to be calculated, about which nothing is as yet known at the present time.

For qualifying the similarity, e.g., the Euclidean distance

$$d((Z, R), (\tilde{Z}, \tilde{R})) = \sqrt{(Z - \tilde{Z})^2 + (R - \tilde{R})^2}$$

is used at the payment reserve level in the prior art. But also with the Euclidean distance there are many possibilities for finding for a given claim  $(P_{i,1,f}, P_{i,2,f}, \dots, P_{i,K+1-i,f})$  the closest most similar claim of an earlier incidence year, i.e., the claim  $\sim P_{1,\dots}, \sim P_k$  with  $k > K+1-i$ , for which either

$$5 \quad \sum_{j=1}^{K+1-i} d(P_{ijf}, \tilde{P}_j) \quad (\text{sum of all previous distances})$$

or

$$\sum_{j=1}^{K+1-i} j \cdot d(P_{ijf}, \tilde{P}_j) \quad (\text{weighted sum of all distances})$$

or

$$\max_{1 \leq j \leq K+1-i} d(P_{ijf}, \tilde{P}_j) \quad (\text{maximum distance})$$

10

or

$$d(P_{i,K+1-i,f}, \tilde{P}_{K+1-i}) \quad (\text{current distance})$$

is minimal.

In the example of the Mack method, normally the current distance is used. This means that for a claim  $(P_1, \dots, P_k)$ , the handling of which is known up to the k-th development year, of all other claims  $(\tilde{P}_1, \dots, \tilde{P}_j)$ , the development of which is known at least up to the development year  $j \geq k + 1$ , the one considered as the most similar is the one for which the current distance  $d(P_k, \tilde{P}_k)$  is smallest.

The claim  $(P_1, \dots, P_k)$  is now continued as is the case for its closest-distance "model"  $(\tilde{P}_1, \dots, \tilde{P}_k, \tilde{P}_{k+1}, \dots, \tilde{P}_j)$ . For doing this, there is the possibility of continuing for a single handling year (i.e., up to  $P_{k+1}$ ) or for several development years at the same time (e.g., up to  $P_j$ ). In methods such as the Mack method, for instance, one typically first continues for just one handling year in order to search then again for a new most similar claim, whereby the claim just

continued is continued for a further development year. The next claim found may naturally also again be the same one. For continuation of the damage claims, there are two possibilities. The additive continuation of  $P_k = (Z_k, R_k)$

$$\hat{P}_{k+1} = (\hat{Z}_{k+1}, \hat{R}_{k+1}) = (Z_k + \tilde{Z}_{k+1} - \tilde{Z}_k, R_k + \tilde{R}_{k+1} - \tilde{R}_k),$$

5 and the multiplicative continuation of  $P_k = (Z_k, R_k)$

$$\hat{P}_{k+1} = (\hat{Z}_{k+1}, \hat{R}_{k+1}) = (Z_k \cdot \frac{\tilde{Z}_{k+1}}{\tilde{Z}_k}, R_k \cdot \frac{\tilde{R}_{k+1}}{\tilde{R}_k}).$$

It is easy to see that one of the drawbacks of the prior art, especially of the Mack method, resides, among other things, in the type of continuation of the damage claims. The multiplicative continuation is useful only for so-called  
 10 open claim statuses, i.e.,  $Z_k > 0, R_k > 0$ . In the case of probable claim statuses  $P_k = (0, R_k), R_k > 0$ , the multiplicative continuation must be diversified since otherwise no continuation takes place. Moreover if  $\tilde{Z}_k = 0$  or  $\tilde{R}_k = 0$ , a division by 0 takes place. Similarly, if  $\tilde{Z}_k$  or  $\tilde{R}_k$  is small, the multiplicative method may easily lead to unrealistically high continuations. This does not permit a  
 15 consistent treatment of the cases. This means that the reserve  $R_k$  cannot be simply continued in this case. In the same way, an adjusted claim status  $P_k = (Z_k, 0), Z_k > 0$  can likewise not be further developed. One possibility is simply to leave it unchanged. However, a revival of a claim is thereby prevented. At best it could be continued on the basis of the closest adjusted model, which likewise  
 20 does not permit a consistent treatment of the cases. Also with the additive continuation, probable claim statuses should meaningfully be continued only on the basis of a likewise probable model in order to minimize the Euclidean distance and to guarantee a corresponding qualification of the similarity. An analogous drawback arises in the case of adjusted claim statuses, if a revival is  
 25 supposed to be allowed and negative reserves are supposed to be avoided. Quite generally, the additive method can easily lead to negative payments and/or reserves. In addition, in the prior art, a claim  $P_k$  cannot be continued if no corresponding model exists without further assumptions being inserted into the method. As an example thereof is an open claim  $P_k$  when in the same  
 30 handling year  $k$  there is no claim from previous incidence years in which  $\tilde{P}_k$  is likewise open. A way out of the dilemma can be found in that, for this case,  $P_k$

is left unchanged, i.e.  $\hat{P}_{k+1} = P_k$ , which of course does not correspond to any true continuation.

Thus, all in all, in the prior art every current claim status  $P_{i,K+1-i,f} = (Z_{i,K+1-i,f}, R_{i,K+1-i,f})$  is further developed step by step either additively or  
 5 multiplicatively up to the end of development and/or handling after K-development years. Here, in each step, the nearest, according to the Euclidean distance in each case, model claim status of the same claim status type (probable, open, or adjusted) is ascertained, and the claim status to be continued is continued either additively or multiplicatively according to the  
 10 further development of the model claim. For the Mack method, it is likewise sensible always to take into consideration as model only actually observed claim developments  $\tilde{P}_k \rightarrow \tilde{P}_{k+1}$  and no extrapolated, i.e., developed claim developments since otherwise a correlation and/or a corresponding bias of the events is not to be avoided. Conversely, however, the drawback is maintained  
 15 that already known information of events is lost.

From the construction of the prior art methods it is immediately clear that the methods can also be applied separately, on the one hand to the triangle of payments, on the other hand to the triangle of reserves. Naturally, with the way of proceeding described, other possibilities could also be permitted  
 20 in order to find the closest claim status as model in each case. However, this would have an effect particularly on the distribution freedom of the method. It may thereby be said that in the prior art, the above-mentioned systematic problems cannot be eliminated even by respective modifications, or at best only in that further model assumptions are inserted into the method. Precisely in the  
 25 case of complex dynamically non-linear processes, however, as e.g. the development of damage claims, this is not desirable in most cases. Even putting aside the mentioned drawbacks, it must still always be determined, in the conventional method according to T. Mack, when two claims are similar and what it means to continue a claim, whereby, therefore, minimum basic  
 30 assumptions and/or model assumptions must be made. In the prior art, however, not only is the choice of Euclidean metrics arbitrary, but also the choice between the mentioned multiplicative and additive methods. Furthermore, the estimation of error is not defined in detail in the prior art. It is



true that it is conceivable to define an error, e.g., based on the inverse distance. However, this is not disclosed in the prior art. An important drawback of the prior art is also, however, that each event must be compared with all the previous ones in order to be able to be continued. The expenditure increases  
 5 linearly with the number of years and linearly with the number of claims in the portfolio. When portfolios are aggregated, the computing effort and the memory requirement increase accordingly.

Neural networks are fundamentally known in the prior art, and are used, for instance, for solving optimization problems, image recognition (pattern  
 10 recognition), in artificial intelligence, etc. Corresponding to biological nerve networks, a neural network consists of a plurality of network nodes, so-called neurons, which are interconnected via weighted connections (synapses). The neurons are organized in network layers (layers) and interconnected. The individual neurons are activated in dependence upon their input signals and  
 15 generate a corresponding output signal. The activation of a neuron takes place via an individual weight factor by the summation over the input signals. Such neural networks are adaptive by systematically changing the weight factors as a function of given exemplary input and output values until the neural network shows a desired behavior in a defined, predictable error span, such as the  
 20 prediction of output values for future input values, for example. Neural networks thereby exhibit adaptive capabilities for learning and storing knowledge and associative capabilities for the comparison of new information with stored knowledge. The neurons (network nodes) may assume a resting state or an excitation state. Each neuron has a plurality of inputs and just one  
 25 output which is connected in the inputs of other neurons of the following network layer or, in the case of an output node, represents a corresponding output value. A neuron enters the excitation state when a sufficient number of the inputs of the neuron are excited over a certain threshold value of the neuron, i.e., if the summation over the inputs reaches a certain threshold value.  
 30 In the weights of the inputs of a neuron and in the threshold value of the neuron, the knowledge is stored through adaptation. The weights of a neural network are trained by means of a learning process (see, e.g., G. Cybenko, "Approximation by Superpositions of a sigmoidal function," *Math. Control, Sig. Syst.*, 2, 1989, pp. 303-314; M. T. Hagan, M. B. Menhaj, "Training Feed-forward

Networks with the Marquardt Algorithm," *IEEE Transactions on Neural Networks*, Vol. 5, No. 6, pp. 989-993, November 1994; K. Hornik, M. Stinchcombe, H. White, "Multilayer Feed-forward Networks are Universal Approximators," *Neural Networks*, 2, 1989, pp. 359-366, etc.).

5           It is a task of this invention to propose a new system and method for automated experience rating of events and/or loss reserving which does not exhibit the above-mentioned drawbacks of the prior art. In particular, an automated, simple, and rational method shall be proposed in order to develop a given claim further with an individual increase and/or factor so that  
 10       subsequently all the information concerning the development of a single claim is available. With the method, as few assumptions as possible shall be made from the outset concerning the distribution, and at the same time the maximum possible information on the given cases shall be exploited.

              According to the present invention, this goal is achieved in particular  
 15       by means of the elements of the independent claims. Further advantageous embodiments follow moreover from the dependent claims and the description.

              In particular, these goals are achieved by the invention in that development values  $P_{i,k,f}$  having development intervals  $k=1,\dots,K$  are assigned to a certain event  $P_{i,f}$  of an initial time interval  $i$ , wherein  $K$  is the last known  
 20       development interval is, with  $i=1,\dots,K$ , and for the events  $P_{1,f}$  all development values  $P_{1kf}$  are known, at least one neural network being used for determining the development values  $P_{i,K+2-i,f},\dots,P_{ikf}$ . In the case of certain events, e.g., the initial time interval can be assigned to an initial year, and the development intervals can be assigned to development years. The development values  $P_{ikf}$   
 25       of the various events  $P_{i,f}$  can, according to their initial time interval, be scaled by means of at least one scaling factor. The scaling of the development values  $P_{ikf}$  has the advantage, among others, that the development values are comparable at differing points in time. This variant embodiment further has the advantage, among others, that for the automated experience rating no model assumptions  
 30       need be presupposed, e.g. concerning value distributions, system dynamics, etc. In particular, the experience rating is free of proximation preconditions, such as the Euclidean measure, etc., for example. This is not possible in this

way in the prior art. In addition, the entire information of the data sample is used, without the data records' being cumulated. The complete information concerning the individual events is kept in each step, and can be called up again at the end. The scaling has the advantage that data records of differing  
 5 initial time intervals receive comparable orders of magnitude, and can thus be better compared.

In one variant embodiment, for determining the development values  $P_{i,K-(i-j)+1,f}$  ( $i-1$ ) neural networks  $N_{i,j}$  are generated iteratively with  $j=1,\dots,(i-1)$  for each initial time interval and/or initial year  $i$ , the neural network  $N_{i,j+1}$  depending  
 10 recursively on the neural network  $N_{i,j}$ . For weighting a certain neural network  $N_{i,j}$ , the development values  $P_{p,q,f}$  can be used, for example, with  $p=1,\dots,(i-1)$  and  $q=1,\dots,K-(i-j)$ . This variant embodiment has the advantage, among others, that, as in the preceding variant embodiment, the entire information of the data sample is used, without the data records' being cumulated. The complete  
 15 information concerning the individual events is maintained in each step, and can be called up again at the end. By means of a minimizing of a globally introduced error, the networks can be additionally optimized.

In another variant embodiment, the neural networks  $N_{i,j}$  are identically trained for identical development years and/or development intervals  
 20  $j$ , the neural network  $N_{i+1,j=i}$  being generated for an initial time interval and/or initial year  $i+1$ , and all other neural networks  $N_{i+1,j<i}$  being taken over from previous initial time intervals and/or initial years. This variant embodiment has the advantage, among others, that only known data are used for the experience rating, and certain data are not used further by the system, whereby the  
 25 correlation of the errors or respectively of the data is prevented.

In a still different variant embodiment, events  $P_{i,f}$  with initial time interval  $i<1$  are additionally used for determination, all development values  $P_{i<1,k,f}$  for the events  $P_{i<1,f}$  being known. This variant embodiment has the  
 30 advantage, among others, that by means of the additional data records the neural networks can be better optimized, and their errors can be minimized.

In a further variant embodiment, for the automated experience rating and/or loss reserving, development values  $P_{i,k,f}$  with development intervals  $k=1,\dots,K$  are stored assigned to a certain event  $P_{i,f}$  of an initial time interval  $i$ , in which  $i = 1,\dots,K$ , and  $K$  is the last known development interval, and in which for the first initial time interval all development values  $P_{1,k,f}$  are known, for each initial time interval  $i=2,\dots,K$  by means of iterations  $j=1,\dots,(i-1)$  upon each iteration  $j$  in a first step a neural network  $N_{i,j}$  being generated having an input layer with  $K-(i-j)$  input segments and an output layer, which input segments comprise at least one input neuron and are assigned to a development value  $P_{i,k,f}$ , in a second step the neural network  $N_{i,j}$  with the available events  $P_{i,f}$  of all initial time intervals  $m=1,\dots,(i-1)$  being weighted by means of the development values  $P_{m,1..K-(i-j),f}$  as input and  $P_{m,1..K-(i-j)+1,f}$  as output, and in a third step by means of the neural network  $N_{i,j}$  the output values  $O_{i,f}$  being determined for all events  $P_{i,f}$  of the initial time interval  $i$ , the output value  $O_{i,f}$  being assigned to the development value  $P_{i,K-(i-j)+1,f}$  of the event  $P_{i,f}$ , and the neural network  $N_{i,j}$  being dependent recursively on the neural network  $N_{i,j+1}$ . In the case of certain events, e.g., the initial time interval can be assigned to an initial year, and the development intervals assigned to development years. This variant embodiment has the same advantages, among others, as the preceding variant embodiments.

In one variant embodiment, a system comprises neural networks  $N_i$  each having an input layer with at least one input segment and an output layer, which input and output layer comprises a plurality of neurons which are interconnected in a weighted way, the neural networks  $N_i$  being iteratively producible by means of a data processing unit through software and/or hardware, a neural network  $N_{i+1}$  depending recursively on the neural network  $N_i$ , and each network  $N_{i+1}$  comprising in each case one input segment more than the network  $N_i$ , each neural network  $N_i$ , beginning with the neural network  $N_1$ , being trainable by means of a minimization module through minimizing of a locally propagated error, and the recursive system of neural networks being trainable by means of a minimization module through minimization of a globally propagated error based upon the local errors of the neural networks  $N_i$ . This variant embodiment has the advantage, among others, that the recursively generated neural networks can be additionally optimized by means of the global

error. Among other things, it is the combination of the recursive generation of the neural network structure with a double minimization by means of locally propagated error and globally propagated error which results in the advantages of the variant embodiment.

5 In another variant embodiment, the output layer of the neural network  $N_i$  is connected in an assigned way to at least one input segment of the input layer of the neural network  $N_{i+1}$ . This variant embodiment has the advantage, among others, that the system of neural networks can in turn be interpreted as a neural network. Thus partial networks of a whole network may  
10 be locally weighted, and also in the case of global learning can be checked and monitored in their behavior by the system by means of the corresponding data records. This has not been possible until now in this way in the prior art.

At this point, it shall be stated that besides the method according to the invention, the present invention also relates to a system for carrying out this  
15 method. Furthermore, it is not limited to the said system and method, but equally relates to recursively nested systems of neural networks and a computer program product for implementing the method according to the invention.

Variant embodiments of the present invention are described below  
20 on the basis of examples. The examples of the embodiments are illustrated by the following accompanying figures:

Figure 1 shows a block diagram which reproduces schematically the training and/or determination phase or presentation phase of a neural network for determining the event value  $P_{2,5,f}$  of an event  $P_f$  in an upper 5x5 matrix, i.e.,  
25 with  $K=5$ . The dashed line T indicates the training phase, and the solid line R the determination phase after learning.

Figure 2 likewise shows a block diagram which, like Figure 1, reproduces schematically the training and/or determination phase of a neural network for determining the event value  $P_{3,4,f}$  for the third initial year.

Figure 3 shows a block diagram which, like Figure 1, reproduces schematically the training and/or determination phase of a neural network for determining the event value  $P_{3,5,f}$  for the third initial year.

Figure 4 shows a block diagram which schematically shows only the training phase for determining  $P_{3,4,f}$  and  $P_{3,5,f}$ , the calculated values  $P_{3,4,f}$  being used for training the network for determining  $P_{3,5,f}$ .

Figure 5 shows a block diagram which schematically shows the recursive generation of neural networks for determining the values in line 3 of a 5x5 matrix, two networks being generated.

Figure 6 shows a block diagram which schematically shows the recursive generation of neural networks for determining the values in line 5 of a 5x5 matrix, four networks being generated.

Figure 7 shows a block diagram which likewise shows schematically a system according to the invention, the training basis being restricted to the known event values  $A_{ij}$ .

Figures 1 to 7 illustrate schematically an architecture which may be used for implementing the invention. In this embodiment example, a certain event  $P_{i,f}$  of an initial year  $i$  includes development values  $P_{ikf}$  for the automated experience rating of events and/or loss reserving. The index  $f$  runs over all events  $P_{i,f}$  for a certain initial year  $i$  with  $f = 1, \dots, F_j$ . The development value  $P_{ikf} = (Z_{ikf}, R_{ikf}, \dots)$  is any vector and/or  $n$ -tuple of development parameters  $Z_{ikf}$ ,  $R_{ikf}$ ,  $\dots$ , which is supposed to be developed for an event. Thus, for example, in the case of insurance for a damage event  $P_{ikf}$ ,  $Z_{ikf}$  can be the payment status,  $R_{ikf}$  the reserve status, etc. Any desired further relevant parameters for an event are conceivable without this affecting the scope of protection of the invention. The development years  $k$  proceed from  $k=1, \dots, K$ , and the initial years  $i = 1, \dots, I$ .  $K$  is the last known development year. For the first initial year  $i = 1$ , all development values  $P_{1kf}$  are given. As already indicated, for this example the number of initial years  $I$  and the number of development years  $K$  are supposed to be the same, i.e.,  $I = K$ . However, it is quite conceivable that  $I \neq K$ , without

the method or the system being thereby limited.  $P_{ikf}$  is therefore an n-tuple consisting of the sequence of dots and/or matrix elements

$$(Z_{ikn}, R_{ikn}, \dots) \quad \text{with } k = 1, 2, \dots, K$$

With  $I = K$  the result is thereby a quadratic upper triangular matrix  
 5 and/or block triangular matrix for the known development values  $P_{ikf}$

$$\begin{pmatrix} P_{11f=1..F_1} & P_{12f=1..F_1} & P_{13f=1..F_1} & P_{14f=1..F_1} & P_{15f=1..F_1} \\ P_{21f=1..F_2} & P_{22f=1..F_2} & P_{23f=1..F_2} & P_{24f=1..F_2} & \\ P_{31f=1..F_3} & P_{32f=1..F_3} & P_{33f=1..F_3} & & \\ P_{41f=1..F_4} & P_{42f=1..F_4} & & & \\ P_{51f=1..F_5} & & & & \end{pmatrix}$$

again with  $f=1, \dots, F_i$  going over all events for a certain initial year.

Thus, the lines of the matrix are assigned to the initial years and the columns of the matrix to the development years. In the embodiment example,  $P_{ikf}$  shall be  
 10 limited to the example of damage events with insurance since in particular the method and/or the system is very suitable, e.g., for the experience rating of insurance contracts and/or excess loss reinsurance contracts. It must be emphasized that the matrix elements  $P_{ikf}$  may themselves again be vectors and/or matrices, whereupon the above matrix becomes a corresponding block  
 15 matrix. The method and system according to the invention is, however, suitable for experience rating and/or for extrapolation of time-delayed non-linear processes quite generally. That being said,  $P_{ikf}$  is a sequence of dots

$$(Z_{ikn}, R_{ikn}, \dots) \quad \text{with } k = 1, 2, \dots, K$$

at the payment reserve level, the first  $K+1-i$  dots of which are known,  
 20 and the still unknown dots  $(Z_{i,K+2-i,f}, R_{i,K+2-i,f}), \dots, (Z_{iKf}, R_{iKf})$ , are supposed to be predicted. If, for this example,  $P_{ikf}$  is divided into payment level and reserve

level, the result obtained analogously for the payment level is the triangular matrix

$$\begin{pmatrix} Z_{11f} & Z_{12f} & Z_{13f} & Z_{14f} & Z_{15f} \\ Z_{21f} & Z_{22f} & Z_{23f} & Z_{24f} & \\ Z_{31f} & Z_{32f} & Z_{33f} & & \\ Z_{41f} & Z_{42f} & & & \\ Z_{51f} & & & & \end{pmatrix}$$

5 and for the reserve level the triangular matrix

$$\begin{pmatrix} R_{11f} & R_{12f} & R_{13f} & R_{14f} & R_{15f} \\ R_{21f} & R_{22f} & R_{23f} & R_{24f} & \\ R_{31f} & R_{32f} & R_{33f} & & \\ R_{41f} & R_{42f} & & & \\ R_{51f} & & & & \end{pmatrix}$$

Thus, in the experience rating of damage events, the development of each individual damage event  $f_i$  is known from the point in time of the report of damage in the initial year  $i$  until the current status (current development year  $k$ ) or until adjustment. This information may be stored in a database, which database may be called up, e.g., via a network by means of a data processing unit. However, the database may also be accessible directly via an internal data bus of the system according to the invention, or be read out otherwise.

15 In order to use the data in the example of the claims, the triangular matrices are scaled in a first step, i.e., the damage values must first be made comparable in relation to the assigned time by means of the respective inflation values. The inflation index may likewise be read out of corresponding databases or entered in the system by means of input units. The inflation index for a country may, for example, look like the following:

Year	Inflation Index (%)	Annual Inflation Value
1989	100	1.000
1990	105.042	1.050



1991	112.920	1.075
1992	121.429	1.075
1993	128.676	1.060
1994	135.496	1.053
1995	142.678	1.053
1996	148.813	1.043
1997	153.277	1.030
1998	157.109	1.025
1999	163.236	1.039
2000	171.398	1.050
2001	177.740	1.037
2002	185.738	1.045

Further scaling factors are just as conceivable, such as regional dependencies, etc., for example. If damage events are compared and/or extrapolated in more than one country, respective national dependencies are added. For the general, non-insurance-specific case, the scaling may also relate to dependencies such as e.g. mean age of populations of living beings, influences of nature, etc. etc..

For the automated determination of the development values  $P_{i,K+2-i,f}, \dots, P_{i,K,f} = (Z_{i,K+2-i,f}, R_{i,K+2-i,f}), \dots, (Z_{i,K,f}, R_{i,K,f})$ , the system and/or method comprises at least one neural network. As neural networks, e.g., conventional static and/or dynamic neural networks may be chosen, such as, for example, feed-forward (heteroassociative) networks such as a perceptron or a multi-layer perceptron (MLP), but also other network structures, such as, e.g., recurrent network structures, are conceivable. The differing network structure of the feed-forward networks in contrast to networks with feedback (recurrent networks) determines the way in which information is processed by the network. In the case of a static neural network, the structure is supposed to ensure the replication of static characteristic fields with sufficient approximation quality. For this embodiment example let multilayer perceptrons be chosen as an example. An MLP consists of a number of neuron layers having at least one input layer and one output layer. The structure is directed strictly forward, and

belongs to the group of feed-forward networks. Neural networks quite generally map an  $m$ -dimensional input signal onto an  $n$ -dimensional output signal. The information to be processed is, in the feed-forward network considered here, received by a layer having input neurons, the input layer. The input neurons

5 process the input signals, and forward them via weighted connections, so-called synapses, to one or more hidden neuron layers, the hidden layers. From the hidden layers, the signal is transmitted, likewise by means of weighted synapses, to neurons of an output layer which, in turn, generate the output signal of the neural network. In a forward directed, completely connected MLP,

10 each neuron of a certain layer is connected to all neurons of the following layer. The choice of the number of layers and neurons (network nodes) in a particular layer is, as usual, to be adapted to the respective problem. The simplest possibility is to find out the ideal network structure empirically. In so doing, it is to be heeded that if the number of neurons chosen is too large, the network,

15 instead of learning, works purely image-forming, while with too small a number of neurons it comes to correlations of the mapped parameters. Expressed differently, the fact is that if the number of neurons chosen is too small, the function can possibly not be represented. However, upon increasing the number of hidden neurons, the number of independent variables in the error

20 function also increases. This leads to more local minima and to the greater probability of landing in precisely one of these minima. In the special case of back propagation, this problem can be at least minimized, e.g. by means of simulated annealing. In simulated annealing, a probability is assigned to the states of the network. In analogy to the cooling of liquid material from which

25 crystals are produced, a high initial temperature  $T$  is chosen. This is gradually reduced, the lower the slower. In analogy to the formation of crystals from liquid, it is assumed that if the material is allowed to cool too quickly, the molecules do not arrange themselves according to the grid structure. The crystal becomes impure and unstable at the locations affected. In order to

30 present this, the material is allowed to cool down so slowly that the molecules still have enough energy to jump out of local minimum. In the case of neural networks, nothing different is done: additionally, the magnitude  $T$  is introduced in a slightly modified error function. In the ideal case, this then converges toward a global minimum.

For the application to experience rating, neural networks having an at least three-layered structure have proved useful in MLP. That means that the networks comprise at least one input layer, a hidden layer, and an output layer. Within each neuron, the three processing steps of propagation, activation, and output take place. As output of the  $i$ -th neuron of the  $k$ -th layer there results

$$o_i^k = f_i^k \left( \sum_j w_{i,j}^k \cdot o_{i,j}^{k-1} + b_{i,j}^k \right)$$

whereby e.g. for  $k=2$ , as range of the controlled variable  $j=1,2,\dots,N_1$  is valid; designated with  $N_1$  is the number of neurons of the layer  $k-1$ ,  $w$  as weight, and  $b$  as bias (threshold value). Depending upon the application, the bias  $b$  may be chosen the same or different for all neurons of a certain layer. As activation function, e.g., a log-sigmoidal function may be chosen, such as

$$f_i^k(\xi) = \frac{1}{1 + e^{-\xi}}$$

The activation function (or transfer function) is inserted in each neuron. Other activation functions such as tangential functions, etc., are, however, likewise possible according to the invention. With the back-propagation method, however, it is to be heeded that a differentiable activation function <is used>, such as e.g. a sigmoid function, since this is a prerequisite for the method. That is, therefore, binary activation function as e.g.

$$f(x) := \begin{cases} 1 & \text{if } x > 0 \\ 0 & \text{if } x \leq 0 \end{cases}$$

do not work for the back-propagation method. In the neurons of the output layer, the outputs of the last hidden layer are summed up in a weighted way. The activation function of the output layer may also be linear. The entirety of the weightings  $W_{i,j}^k$  and bias  $B_{i,j}^k$  combined in the parameter- and/or weighting matrices determine the behavior of the neural network structure

$$W^k = (w_{i,j}^k) \in \mathfrak{R}^{N \cdot N_k}$$

Thus the result is

$$o^k = B^k + W^k \cdot \left( 1 + e^{- (B^{k-1} + W^{k-1} \cdot u)} \right)^{-1}$$

The way in which the network is supposed to map an input signal onto an output signal, i.e., the determination of the desired weights and bias of the network, is achieved by training the network by means of training patterns.  
5 The set of training patterns (index  $\mu$ ) consists of the input signal

$$Y^\mu = [y_1^\mu, y_2^\mu, \dots, y_{N_1}^\mu]$$

and an output signal

$$U^\mu = [u_1^\mu, u_2^\mu, \dots, u_{N_1}^\mu]$$

10 In this embodiment example with the experience rating of claims, the training patterns comprise the known events  $P_{i,f}$  with the known development values  $P_{ikf}$  for all  $k$ ,  $f$ , and  $i$ . Here the development values of the events to be extrapolated may naturally not be used for training the neural networks since the output value corresponding to them is lacking.

15 At the start of the learning operation, the initialization of the weights of the hidden layers, thus in this exemplary example of the neurons, is carried out, e.g., by means of a log-sigmoidal activation function, e.g. according to Nguyen-Widrow (D. Nguyen, B. Widrow, "Improving the Learning Speed of 2-Layer Neural Networks by Choosing Initial Values of Adaptive Weights,"  
20 *International Joint Conference of Neural Networks*, Vol. 3, pp. 21-26, July 1990). If a linear activation function has been chosen for the neurons of the output layer, the weights may be initialized, e.g., by means of a symmetrical random number generator. For training the network, various prior art learning methods may be used, such as e.g. the back-propagation method, learning  
25 vector quantization, radial basis function, Hopfield algorithm, or Kohonen algorithm, etc. The task of the training method consists in determining the synapses weights  $w_{i,j}$  and bias  $b_{i,j}$  within the weighting matrix  $W$  and/or the bias

matrix B in such a way that the input patterns  $Y^\mu$  are mapped onto the corresponding output patterns  $U^\mu$ . For judging the learning stage, the absolute quadratic error

$$Err = \frac{1}{2} \sum_{\mu=1}^p \sum_{\lambda=1}^m (u_{eff,\lambda}^\mu - u_{soll,\lambda}^\mu)^2 = \sum_{\mu=1}^p Err^\mu$$

- 5 may be used, for example. The error Err then takes into consideration all patterns  $P_{ikf}$  of the training basis in which the actual output signals  $U_{eff}^\mu$  show the target reactions  $U_{soll}^\mu$  specified in the training basis. For this embodiment example, the back-propagation method shall be chosen as the learning method. The back-propagation method is a recursive method for
- 10 optimizing the weight factors  $w_{ij}$ . In each learning step, an input pattern  $Y^\mu$  is randomly chosen and propagated through the network (forward propagation). By means of the above-described error function Err, the error  $Err^\mu$  on the presented input pattern is determined from the output signal generated by the network by means of the target reaction  $U_{soll}^\mu$  specified in the training basis.
- 15 The modifications of the individual weights  $w_{ij}$  after the presentation of the  $\mu$ -th training pattern are thereby proportional to the negative partial derivation of the error  $Err^\mu$  according to the weight  $w_{ij}$  (so-called gradient descent method)

$$\Delta w_{i,j}^\mu \approx \frac{\partial E^\mu}{\partial w_{i,j}}$$

- 20 With the aid of the chain rule, the known adaptation specifications, known as back-propagation rule, for the elements of the weighting matrix in the presentation of the  $\mu$ -th training pattern can be derived from the partial derivation.

$$\Delta w_{i,j}^\mu \equiv s \cdot \delta_i^\mu \cdot u_{eff,j}^\mu$$

with

25 
$$\delta_i^\mu = f'(\xi_i^\mu) \cdot (u_{soll,i}^\mu - u_{eff,i}^\mu)$$

for the output layer, and

$$\delta_i^\mu = f'(\xi_i^\mu) \cdot \sum_k^K \delta_k^\mu w_{k,i}$$

for the hidden layers, respectively. Here the error is propagated through the network in the opposite direction (back propagation) beginning with the output layer and divided among the individual neurons according to the costs-by-cause principle. The proportionality factor  $s$  is called the learning factor. During the training phase, a limited number of training patterns is presented to a neural network, which patterns characterize precisely enough the map to be learned. In this embodiment example, with the experience rating of damage events, the training patterns may comprise all known events  $P_{i,f}$  with the known development values  $P_{ikf}$  for all  $k$ ,  $f$ , and  $i$ . But a selection of the known events  $P_{i,f}$  is also conceivable. If thereafter the network is presented with an input signal which does not agree exactly with the patterns of the training basis, the network interpolates or extrapolates between the training patterns within the scope of the learned mapping function. This property is called the generalization capability of the networks. It is characteristic of neural networks that neural networks possess good error tolerance. This is a further advantage as compared with the prior art systems. Since neural networks map a plurality of (partially redundant) input signals upon the desired output signal(s), the networks prove to be robust toward the failure of individual input signals and/or toward signal noise. A further interesting property of neural networks is their adaptive capability. Hence it is possible in principle to have a once-trained system relearn or adapt permanently/periodically during operation, which is likewise an advantage as compared with the prior art systems. For the learning method, other methods may naturally also be used, such as e.g. a method according to Levenberg-Marquardt (D. Marquardt, "An Algorithm for least square estimation of non-linear Parameters," *J. Soc. Ind. Appl. Math.*, pp.431-441, 1963, as well as M.T. Hagan, M.B. Menhaj, "Training Feed-forward Networks with the Marquardt Algorithm," *IEEE-Transactions on Neural Networks*, Vol. 5, No. 6, pp.989-993, November 1994). The Levenberg-Marquardt method is a combination of the gradient method and the Newton method, and has the advantage that it converges faster than the above-

mentioned back-propagation method, but needs a greater storage capacity during the training phase.

In the embodiment example, for determining the development values  $P_{i,K-(i-j)+1,f}$  for each initial year  $i$  ( $i-1$ ) neural networks  $N_{i,j}$  are generated iteratively.  $j$  indicates, for a certain initial year  $i$ , the number of iterations, with  $j=1, \dots, (i-1)$ . Thereby, for the  $i$ -st initial year  $i-1$ , neural networks  $N_{i,j}$  are generated. The neural network  $N_{i,j+1}$  depends recursively here from the neural network  $N_{i,j}$ . For weighting, i.e., for training, a certain neural network  $N_{i,j}$ , e.g., all development values  $P_{p,q,f}$  with  $p=1, \dots, (i-1)$  and  $q=1, \dots, K-(i-j)$  of the events or losses  $P_{pq}$  may be used. A limited selection may also be useful, however, depending upon the application. The data of the events  $P_{pq}$  may, for instance, as mentioned be read out of a database and presented to the system via a data processing unit. A calculated development value  $P_{i,k,f}$  may, e.g., be assigned to the respective event  $P_{i,f}$  of an initial year  $i$  and itself be presented to the system for determining the next development value (e.g.,  $P_{i,k+1,f}$ ) (Figures 1 to 6), or the assignment takes place only after the end of the determination of all development values  $P$  sought (Figure 7).

In the first case (Figures 1 to 6), as described, development values  $P_{i,k,f}$  with development year  $k=1, \dots, K$  are assigned to a certain event  $P_{i,f}$  of an initial year  $i$ , whereby for the initial years  $i=1, \dots, K$ , and  $K$  are the last known development year. For the first initial year  $i=1$ , all development values  $P_{1,k,f}$  are known. For each initial year  $i=2, \dots, K$  by means of iterations  $j=1, \dots, (i-1)$ , upon each iteration  $j$ , in a first step, a neural network  $N_{i,j}$  is generated with an input layer with  $K-(i,j)$  input segments and an output layer. Each input segment comprises at least one input neuron and/or at least as many input neurons to obtain the input signal for a development value  $P_{i,k,f}$ . The neural networks are automatically generated by the system, and may be implemented by means of hardware or software. In a second step, the neural network  $N_{i,j}$  with the available events  $E_{i,f}$  of all initial years  $m=1, \dots, (i-1)$  are weighted by means of the development values  $P_{m,1 \dots K-(i-j),f}$  as input and  $P_{m,1 \dots K-(i-j)+1,f}$  as output. In a third step, by means of the neural network  $N_{i,j}$ , the output values  $O_{i,f}$  are determined for all events  $P_{i,f}$  of the initial year  $i$ , the output value  $O_{i,f}$  being assigned to the development value  $P_{i,K-(i-j)+1,f}$  of the event  $P_{i,f}$ , and the neural network  $N_{i,j}$

depending recursively on the neural network  $N_{i,j+1}$ . Figure 1 shows the training and/or presentation phase of a neural network for determining the event value  $P_{2,5,f}$  of an event  $P_f$  in an upper 5x5 matrix, i.e., at  $K+5$ . The dashed line T indicates the training phase, and the solid line R indicates the determination phase after learning. Figure 2 shows the same thing for the third initial year for determining  $P_{3,4,f}$  ( $B_{34}$ ), and Figure 3 for determining  $P_{3,5,f}$ . Figure 4 shows only the training phase for determining  $P_{3,4,f}$  and  $P_{3,5,f}$ , the generated values  $P_{3,4,f}$  ( $B_{34}$ ) being used for training the network for determining  $P_{3,5,f}$ .  $A_{ij}$  indicates the known values in the figures, while  $B_{ij}$  displays certain values by means of the networks. Figure 5 shows the recursive generation of the neural networks for determining the values in line 3 of a 5x5 matrix,  $i-1$  networks being generated, thus two. Figure 6, on the other hand, shows the recursive generation of the neural networks for determining the values in line 3 of a 5x5 matrix,  $i-1$  networks again being generated, thus four.

It is important to point out that, as an embodiment example, the assignment of the event values  $B_{ij}$  generated by means of the system may also take place only after determination of all sought development values  $P$ . The newly determined values are then not available as input values for determination of further event values. Figure 7 shows such a method, the training basis being limited to the known event values  $A_{ij}$ . In other words, the neural networks  $N_{ij}$  may be identical for the same  $j$ , the neural network  $N_{i+1,j=i}$  being generated for an initial time interval  $i+1$ , and all other neural networks  $N_{i+1,j<i}$  corresponding to networks of earlier initial time intervals. This means that a network, which was once generated for calculation of a particular event value  $P_{ij}$ , is further used for all event values with an initial year  $a>i$  for the values  $P_{ij}$  with same  $j$ .

In the case of the insurance cases discussed here, different neural networks may be trained, e.g. based on different data. For example, the networks may be trained based on the paid claims, based on the incurred claims, based on the paid and still outstanding claims (reserves) and/or based on the paid and incurred claims. The best neural network for each case may be determined e.g. by means of minimizing the absolute mean error of the predicted values and the actual values. For example, the ratio of the mean



error to the mean predicted value (of the known claims) may be applied to the predicted values of the modeled values in order to obtain the error. For the case where the predicted values of the previous initial years is <sic. are> co-used for calculation of the following initial years, the error must of course be  
 5 correspondingly cumulated. This can be achieved e.g. in that the square root of the sum of the squares of the individual errors of each model is used.

To obtain a further estimate of the quality and/or training state of the neural networks, e.g. the predicted values can also be fitted by means of the mentioned Pareto distribution. This estimation can also be used to determine  
 10 e.g. the best neural network from among neural networks (e.g. paid claims, outstanding claims, etc.) trained with different sets of data (as described in the last paragraph). It thereby follows with the Pareto distribution

$$\chi^2 = \sum \left( \frac{O(i) - T(i)}{E(i)} \right)^2$$

with

$$15 \quad T(i) = Th \left( (1 - P(i))^{(-1/\alpha)} \right)$$

whereby  $\alpha$  of the fit parameters, Th of the threshold parameters (threshold value), T(i) of the theoretical value of the i-th payment demand, O(i) of the observed value of the i-th payment demand, E(i) is the error of the i-th payment demand and P(i) is the cumulated probability of the i-th payment  
 20 demand with

$$P(1) = \left( \frac{1}{2n} \right)$$

and

$$P(i+1) = P(i) + \frac{1}{n}$$

and n the number of payment demands. For the embodiment  
 25 example here, the error of the systems based on the proposed neural networks

was compared with the chain ladder method with reference to vehicle insurance data. The networks were compared once with the paid claims and once with the incurred claims. In order to compare the data, the individual values were cumulated in the development years. The direct comparison showed the following results for the selected example data per 1000

Initial Year	System Based on Neural Networks		Chain Ladder Method	
	Paid Claims (cumulated values)	Incurred Claims (cumulated values)	Paid Claims (cumulated values)	Incurred Claims (cumulated values)
1996	369.795 ± 5.333	371.551 ± 6.929	387.796 ± n/a	389.512 ± n/a
1997	769.711 ± 6.562	789.997 ± 8.430	812.304 ± 0.313	853.017 ± 15.704
1998	953.353 ± 40.505	953.353 ± 30.977	1099.710 ± 6.522	1042.908 ± 32.551
1999	1142.874 ± 84.947	1440.038 ± 47.390	1052.683 ± 138.221	1385.249 ± 74.813
2000	864.628 ± 99.970	1390.540 ± 73.507	1129.850 ± 261.254	1285.956 ± 112.668
2001	213.330 ± 72.382	288.890 ± 80.617	600.419 ± 407.718	1148.555 ± 439.112

The error shown here corresponds to the standard deviation, i.e. the  $\sigma_1$ -error, for the indicated values. In particular for later initial years, i.e. initial years with greater  $i$ , the system based on neural networks shows a clear advantage in the determination of values compared to the prior art methods in that the errors remain substantially stable. This is not the case in the state of the art since the error there does not increase proportionally for increasing  $i$ . For greater initial years  $i$ , a clear deviation in the amount of the cumulated values is demonstrated between the chain ladder values and those which were obtained with the method according to the invention. This deviation is based on the fact that in the chain ladder method the IBNYR (Incurred But Not Yet Reported) losses have been additionally taken into account. The IBNYR damage events would have to be added to the above-shown values of the method according to the invention. For example, for calculation of the portfolio reserves, the IBNYR damage events can be taken into account by means of a separate development (e.g. chain ladder). In reserving for individual losses or in determining loss amount distributions, the IBNYR damage events play no role, however.